

## Lecture 12—Auto-tuning and Gain Scheduling

1. Introduction
2. Tuning Techniques
3. Relay tuning
4. Applications
5. Gain Scheduling
6. How to find schedules
7. Applications
8. Conclusions

## Introduction

- Tuning and adaptation
- Prior knowledge
- Initialization of adaptive controllers
- PID Control
- Operational aspects
- Operator interface
- Views from the field

## Views from the Field

Canadian mill audit. Average paper mill has 2000 loops, 97% use PI the remaining 3% are PID, adaptive etc. Bill Bialkowski CCA'93.

- Default settings
- Poor control performance due to bad tuning
- Poor control performance due to valves, actuators or positioner problems

Process Performance is not as good as you think. D. Ender, Control Engineering 1993.

- More than 30% of installed controllers operate in manual
- More than 30% of the loops actually increase short term variability
- About 25% of the loops use default settings
- About 30% of the loops have equipment problems

## Auto-tuning Techniques

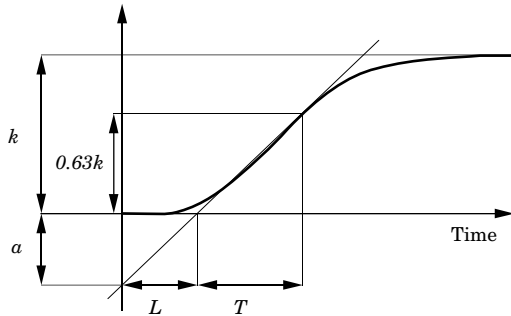
- The Ziegler-Nichols method
- Transient response methods
- Frequency response methods

## Transient Response Methods

The three parameter model

$$G(s) = \frac{k}{1+sT}e^{-sL}$$

Step response methods



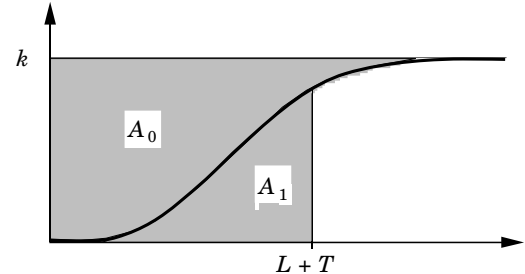
The Ziegler-Nichols method

Controller	$aK_c$	$T_i/L$	$T_d/L$	$T_p/L$
P	1			4
PI	0.9	3		5.7
PID	1.2	2	0.5	3.4

## Difficulties with Ziegler-Nichols

- Difficult to determine parameters
- Too low damping
- Two parameters not enough

Area methods



Parameters are given by

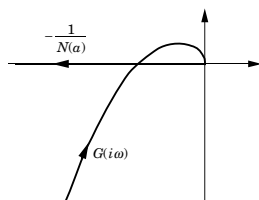
$$T + L = \frac{A_0}{k}$$

$$T = \frac{eA_1}{k}$$

## Ziegler-Nichols Frequency Response Method

Idea: Run a proportional controller, increase gain until the system starts to oscillate. Observe "ultimate gain  $K_u$ , and "ultimate period  $T_u$ .

Interpretation: Find features of frequency response

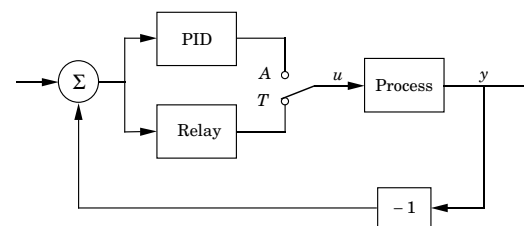


Controller parameters

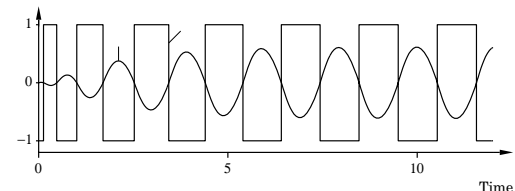
Controller	$K_c/K_u$	$T_i/T_u$	$T_d/T_u$	$T_p/T_u$
P	0.5			1
PI	0.4	0.8		1.4
PID	0.6	0.5	0.12	0.85

## Relay Tuning

The experiment



The results



- Closed loop experiment
- Stable limit cycle for large class of processes
- Much control energy close to  $\omega_{180}$

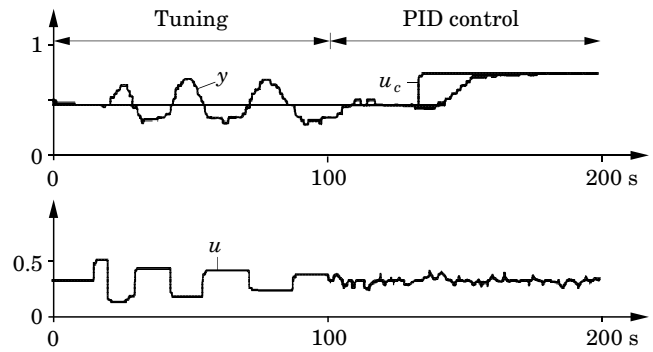
## Practical Issues

- Prior information?
- How to start the experiments
- Feedback to limit the amplitude of the oscillation
- Modified Ziegler-Nichols rules
  - Change values in the tables
  - Use three parameters  $k_u$ ,  $T_u$  and  $K_p$
- How to cope with disturbances
  - Load disturbances
  - Measurement noise
  - Hysteresis

## Automatic Tuning of the Double Tank

Consider the double tank used in our laboratory experiments.

Here is the results obtained with one of our earliest auto-tuners.



## Flow Control

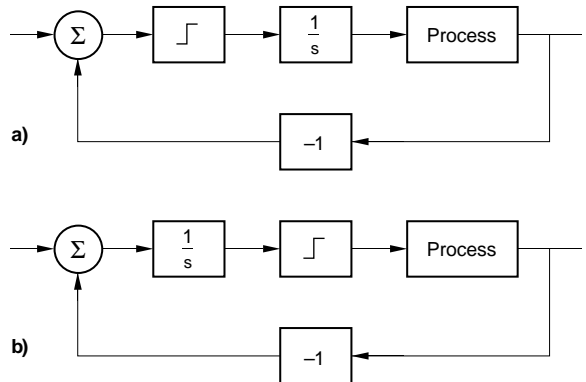
## Temperature Control

## Composition Control

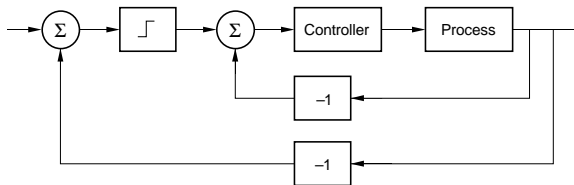
## Adding Dynamics in the Feedback Loop

Other information can be obtained by introducing dynamics in the feedback loop

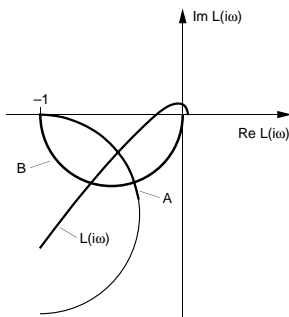
- An integrator gives  $\omega_{90}$
- A differentiator gives  $\omega_{270}$



## Closed Loop Experiments



An integrator can also be added

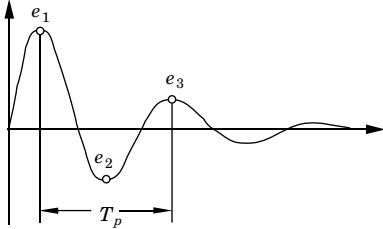


## Summary of Relay Feedback

- Close to industrial operation
- Easy to use
- One-button tuning
- Easy to explain to users
- Works well for standard loops
- Little prior information
- Very robust
- Generates automatically a perturbation signal with a lot of energy at  $\omega_{180}$
- Many possibilities not exploited

## On-line Iteration

Idea: Find features of the online response due to set point or load disturbances. Modify controller settings based on the observed features.



Features: damping  $d$  and overshoot  $o$

$$d = \frac{e_3 - e_2}{e_1 - e_2} \quad o = -\frac{e_2}{e_1}$$

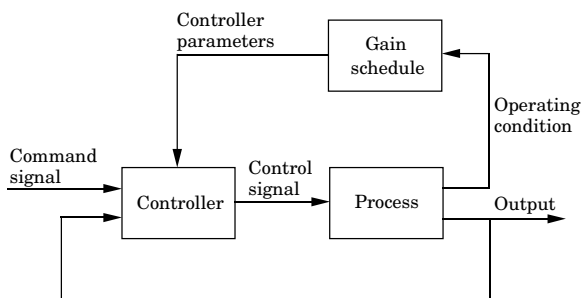
Controller modified based on heuristic rules. Easy for PI more difficult for PID.

- Prior information
- Pre-tuning

## Gain Scheduling

1. What is it?
2. How to find schedules?
3. Applications
4. Conclusions

## Gain Scheduling



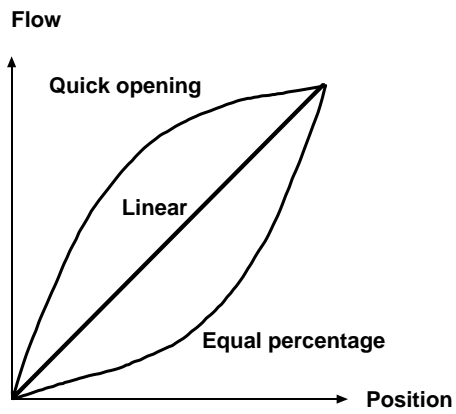
Example of scheduling variables

- Production rate
- Machine speed
- Mach number and dynamic pressure

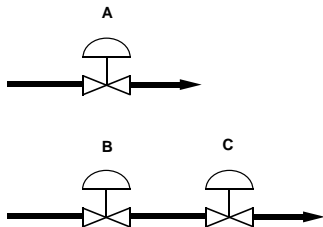
## How to Find Schedules?

- Select scheduling variables
- Make control design for different operating conditions
- Use automatic tuning
- Transformations

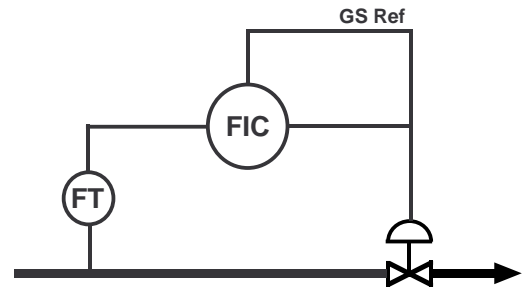
## Valve Characteristics



The valve characteristics depend on the installation

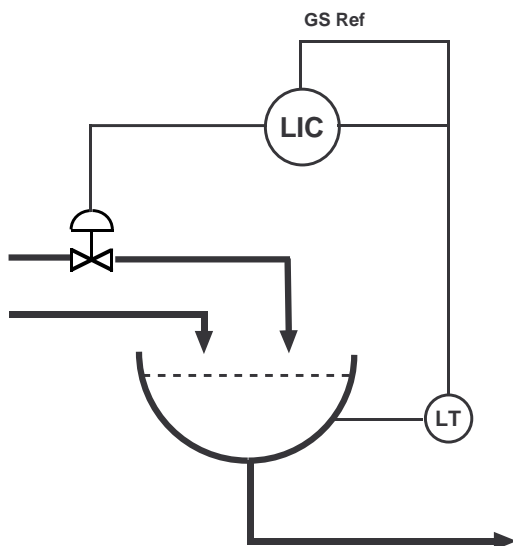


## Schedule on Controller Output



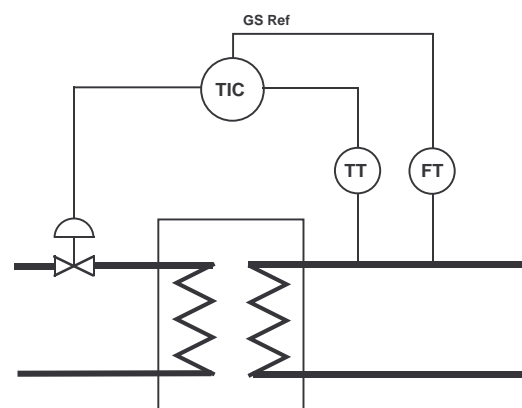
Discuss when this is appropriate

## Schedule on Process Variable



Discuss when this is appropriate

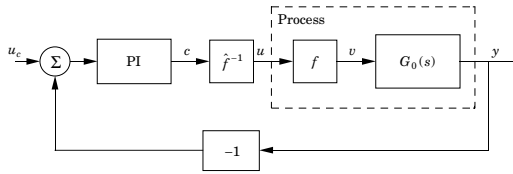
## Schedule on External Variable



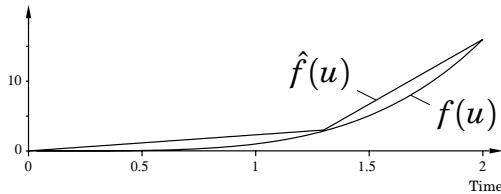
Discuss when this is appropriate

## Nonlinear Valve

A typical process control loop



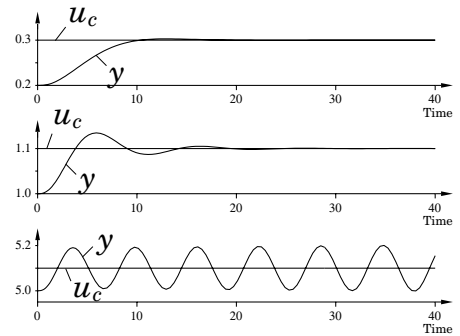
Valve characteristics



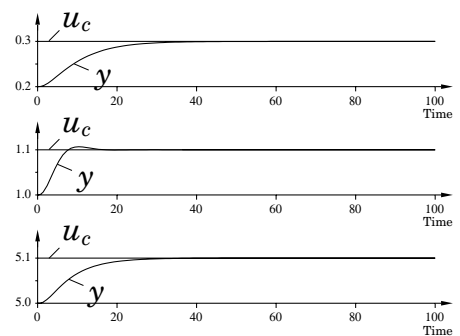
A crude approximation!

## Results

Without gain scheduling

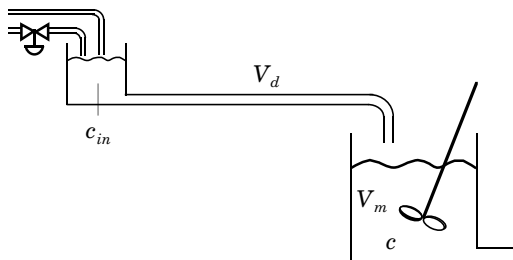


With gain scheduling

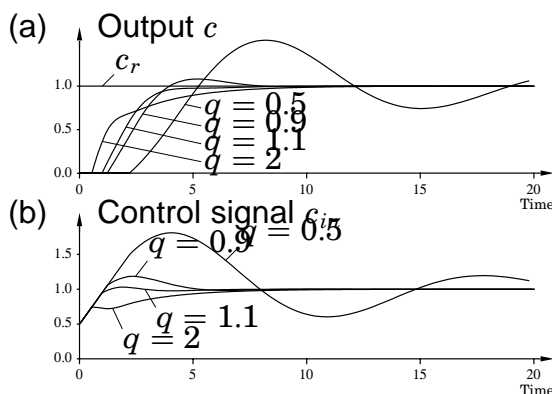


## Concentration Control

System



Performance with changing flow



## Variable Sampling Rate

Process model

$$G(s) = \frac{1}{1+sT} e^{-s\tau}$$

where

$$T = \frac{V_m}{q} \quad \tau = \frac{V_d}{q}$$

Sample the system with period

$$h = \frac{V_d}{nq}$$

The sampled model becomes

$$c(kh+h) = a c(kh) + (1-a)u(kh-nh)$$

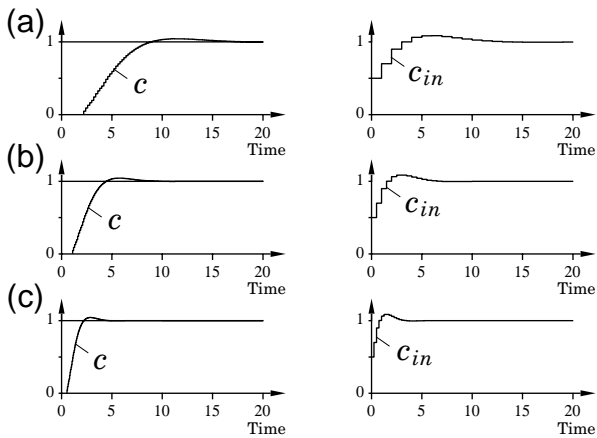
where

$$a = e^{-qh/V_m} = e^{-V-d/(nV_m)}$$

Notice that the sampled equation does not depend on q!!!

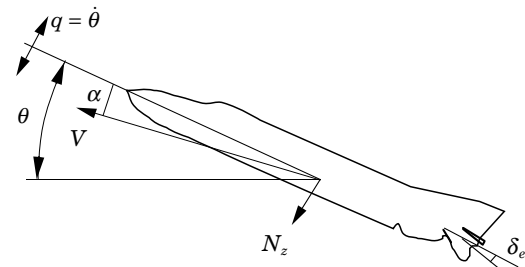
## Results

Digital control with  $h = 1/(2q)$ . The flows are: (a)  $q = 0.5$ ; (b)  $q = 1$ ; (c)  $q = 2$

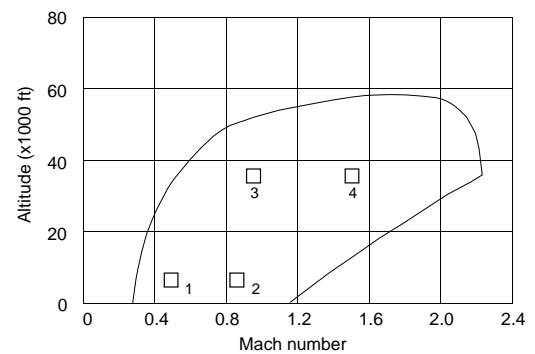


## Flight Control

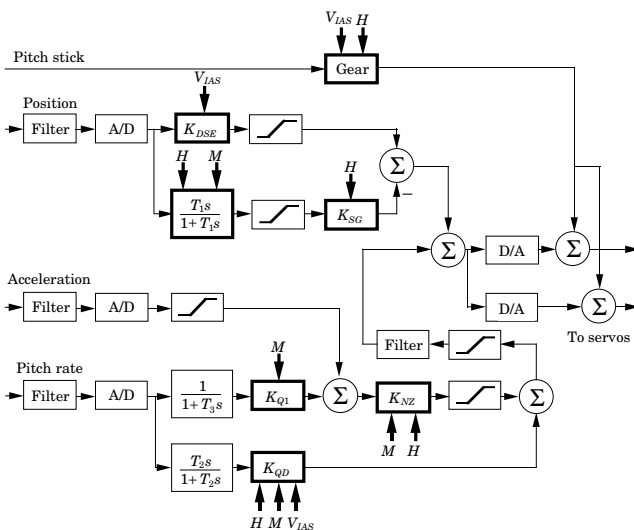
Pitch dynamics



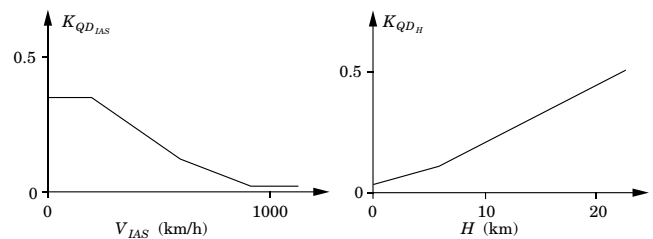
Operating conditions



## The Pitch Control Channel



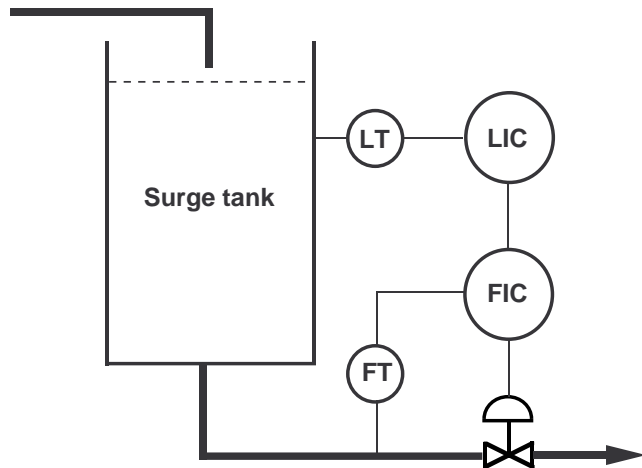
## Schedule of $K_Q$ with Respect to Indicated Airspeed (IAS) and Height (H)





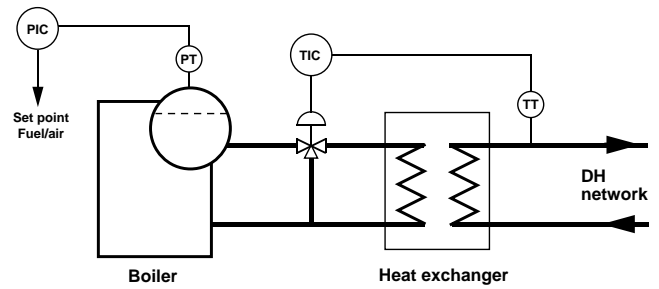
## Surge Tank Control

A surge tank is used to smooth flow variations. The is allowed will fluctuate substantially but it is important that the tank does not become empty or that it overflows.

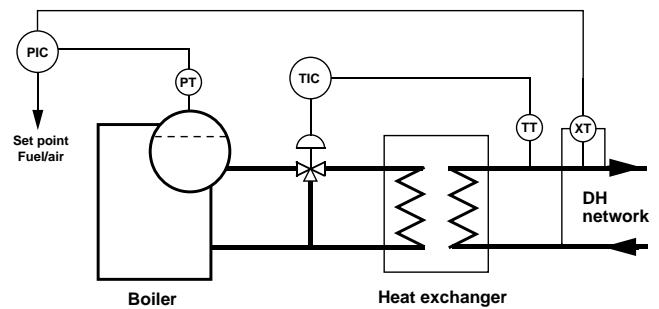


## The Igelsta Power Station

Controller structure before modification



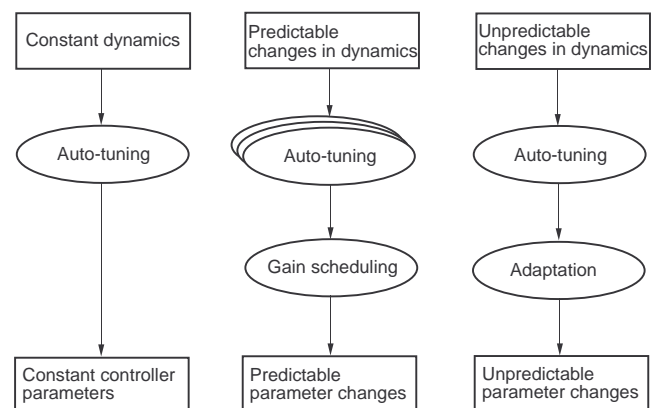
Modified controller structure



## Schedule

Valve Position	$K_c$	$T_i$	$T_d$
0.00-0.15	1.7	95	23
0.15-0.22	2.0	89	22
0.22-0.35	2.9	82	21
0.35-1.00	4.4	68	17

## When to Use Different Techniques?



## Conclusions

- Very useful technique
  - Linearization of nonlinear actuators
  - Surge tank control
  - Control over wide operating ranges
- Requires good models
- Easy to use when combined with auto-tuning
- Good operational experience
- Issues to be considered
  - Choice of scheduling variables
  - Granularity of scheduling tables
  - Interpolation
  - Bumpless parameter changes
  - Operator interfaces